Influence of Inner Diameter and Height of Ring-shaped REBaCuO Bulks on Trapped Field and Mechanical Stress during Field-cooled Magnetization

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***Abstract*—In this paper, the trapped field, B_z, thermal hoop stress, σ_θ^{cool}, by cooling from 300 to 50 K and electromagnetic hoop stress, σ_θ^{FCM}, during field cooled magnetization (FCM) from B_{app} = 6.3 and 9.4 T are investigated numerically for ring-shaped RE-BaCuO bulks with various inner diameters (*I.D.*) and heights (*H*) and reinforced by an Al alloy ring. For simplicity, an identical critical current density, $J_c(B)$, which is a typical value at 50 K, is assumed in the simulation. The B_z value at the center of the ring bulk changes depending on the *I.D.* and *H* values of the ring bulk, which results from the different distribution of the superconducting current. As a result, the total hoop stress, σ_θ^{total}, ($= \sigma_\theta^{cool} + \sigma_\theta^{FCM}$) also changes for each ring bulk and for each B_{app} due to the variation of the σ_θ^{cool} and σ_θ^{FCM} values. The maximum σ_θ^{total} value, which affects the bulk fracture at B_{app} =9.4 T, increases with decreasing the height of ring bulk. These results can present guidelines for designing a trapped-field magnet using ring bulks.**

***Index Terms*—Bulk high-temperature superconductors, finite element method, field-cooled magnetization, mechanical properties, numerical simulation.**

I. Introduction

FOR the practical application of trapped field magnets (TFMs) using superconducting bulks such as RE-Ba-Cu-O (REBaCuO, RE: rare earth element or Y) and MgB_2, it is an important issue to increase the trapped field in the bulk. The trapped field capability of a disk-shaped bulk is proportional to the critical current density, $J_c(B, T)$, and the diameter, as well as the height of the bulk. For field-cooled magnetization (FCM), which is a conventional magnetizing technique, increasing $J_c(B, T)$ by lowering the operating temperature is an effective way to enhance the trapped field. To date, a highest trapped field of 17.6 T has been achieved at 26 K in a disk-shaped GdBaCuO bulk pair reinforced by shrink-fit stainless steel [1]. During the FCM process, however, a large Lorentz force, $\boldsymbol{F}_L$ ($= \boldsymbol{J} \times \boldsymbol{B}$), is generated due to the interaction between the induced current density (J) and the magnetic field (B), and results in fracture of the bulk when the magnetic stress exceeds the mechanical strength of the material. Analytical solutions of the mechanical stresses have been investigated during FCM for the disk and ring bulks with infinite height, in which the Bean's critical state model was mainly used for superconducting characteristics [2] – [4].

A ring-shaped REBaCuO bulk is also useful for practical applications such as nuclear magnetic resonance (NMR) spectrometers and magnetic resonance imaging (MRI) apparatus [5], [6], in which the trapped field enhancement is an ongoing challenge to improve their resolution. In addition to $J_c(B, T)$, the distributions of the trapped field and mechanical stress change depending on the inner diameter (*I.D.*), outer diameter (*O.D.*) and height (*H*) of the ring bulk. Although several experimental and numerical results exist for the trapped field and mechanical stress for the ring-shaped bulk [7] – [10], there have not been systematic investigations for the mechanical stress and the effect of the metal ring reinforcement in the ring bulk with finite height.

In the present paper, the trapped field, B_z, thermal hoop stress, σ_θ^{cool}, by cooling from 300 to 50 K and electromagnetic hoop stress, σ_θ^{FCM}, during FCM from B_{app} = 6.3 and 9.4 T are investigated for ring-shaped REBaCuO bulks (*O.D.* = 64 mm) with various *I.D.* and *H* and reinforced by an aluminum (Al) alloy ring, under the assumption of an identical critical current density, $J_c(B)$, for the bulk. The influence of the shape of the ring bulk on the risk of the mechanical fracture is also discussed.

II. Numerical simulation framework

A three-dimensional (3D) finite element model was constructed, based on our experimental setup for FCM [8] as shown in Fig. 1, for the electromagnetic and mechanical simulation. Five REBaCuO ring bulks 64 mm in O.D. were investigated, in which *I.D.* was changed from 28 to 40 mm and *H* was changed from 20 to 6 mm, as shown in Table I. Each ring bulk was mounted in an Al alloy (A7075-T6) ring 5 mm in

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width (74 mm in *O.D.* and 64.2 mm in *I.D.*) with the same height as the ring bulk using an epoxy resin 0.1 mm in thickness. In the FCM process, the ring bulk was cooled to the magnetizing temperature of T_s = 50 K, based on the experimental setup [5], [6], under initial applied fields of B_{app} = 6.3 and 9.4 T using a solenoid coil (170 mm in *O.D.*, 120 mm in *I.D.* and 200 mm in *H*), and then, the external field was decreased linearly at -0.222 Tmin^{-1} down to zero. The B_{app} value of 6.3 and 9.4 T is equivalent to 270 and 400 MHz, respectively, considering practical NMR resolution. The time step (*TS*) of the descent of the magnetic field during FCM is defined as $TS = 10\ (B_{app} - B_{ex}) / B_{app}$ by 10 steps, in which B_{ex} is the actual time-dependent external field.

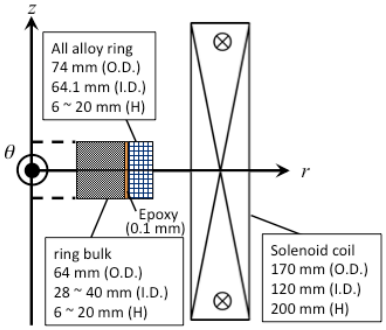

Fig. 1. Cross-sectional view of the numerical model of the ring bulk reinforced by Al alloy ring, which is magnetized using a solenoid coil.

TABLE I
DIMENSIONS OF THE FIVE SIMULATED REBACUO RING BULKS.

Bulk name	O.D. (mm)	I.D. (mm)	H (mm)
Bulk (1)	64	40	20
Bulk (2)	64	28	20
Bulk (3)	64	34	20
Bulk (4)	64	34	12
Bulk (5)	64	34	6

TABLE II
ASSUMED MECHANICAL PARAMETERS OF REBACUO BULK, EPOXY RESIN, AND AL ALLOY USED IN THE NUMERICAL SIMULATION.

	E_Y (GPa)[a]	ν[b]	α (K^{-1})[c]
REBaCuO bulk	100	0.33	6.80 x 10^{-6}
Epoxy resin	3	0.37	4.61 x 10^{-5}
Al alloy (A7075-T6)	78	0.34	1.72 x 10^{-5}

[a]Young's modulus, [b]Poisson ratio, [c]Thermal expansion coefficient

The electromagnetic phenomena during FCM are described elsewhere [10], [11]. The temperature variation during FCM is ignored for simplicity, assuming isothermal conditions. The *E-J* power law is used to simulate the highly non-linear resistivity of the superconductor, where the electric field, *E*, is proportional to J^n, and n = 20 is assumed as a typical value for HTS materials and a good approximation of Bean's critical state model [12]. The $J_c(B)$ characteristics of the bulk were assumed using the following equation [13], [14].

$$J_c(B) = J_{c1} \exp\left(-\frac{B}{B_L}\right) + J_{c2}\frac{B}{B_{max}} \exp\left[\frac{1}{k}\left(1 - \left(\frac{B}{B_{max}}\right)^k\right)\right], \quad (1)$$

where each parameter (J_{c1} = 2.3 x 10^9 A/m^2, J_{c2} = 1.57 x 10^9 A/m^2, B_L = 0.8 T, B_{max} = 4.5 T and k = 1.0) can reproduce actual experimental results at 50 K [15], [16].

The commercial finite element method (FEM) software package, Photo-Eddy (Photon Ltd., Japan), was adapted for the analysis of the trapped field, B_z, and induced current density, J_θ, along the θ-direction in the bulk. Elastic behavior in isotropic materials can be expressed by Hooke's law, and a detailed explanation is provided elsewhere [7], [8]. The nodal force on each node of the meshed elements calculated by Photo-Eddy was exported to the software package, Photo-ELAS (Photon Ltd., Japan), for the analysis of the hoop stress, σ_θ. The assumed mechanical parameters (Young's modulus, E_Y, Poisson ratio, ν, and thermal expansion coefficient, α) of each component used in the mechanical simulation are summarized in Table II, which are assumed to be isotropic and to be in the elastic region.

III. RESULTS OF ELECTROMAGNETIC SIMULATION

Fig. 2(a) shows the *TS* dependence of trapped field at the center of the five ring bulks, B_z ($z = r$ = 0 mm), during FCM from B_{app} = 6.3 T and 9.4 T. The B_z value gradually decreases with increasing *TS* for each case. For each B_{app}, the B_z value at the final step (*TS* = 10) changes depending on the *I.D.* and *H* values. For the ring bulks with identical height of *H* = 20 (bulks (1) - (3)), the final B_z value increases with decreasing *I.D.*. For the bulks with identical *I.D.* = 34 mm, the final B_z value increases with increasing *H*. It should be noted that the final B_z value for bulk (5) (*I.D.* = 34 mm, *H* = 6 mm) is the same for both B_{app} values. These results suggest that the thin bulk was fully magnetized for higher B_{app} than 6.3 T and that the induced supercurrent flows through the entire bulk.

Fig. 2(b) shows the final B_z ($z = r$ = 0 mm) value for the ring bulks with *H* = 20 mm for B_{app} = 6.3 and 9.4 T, as a function of *I.D.*. B_z decreases with increasing *I.D.* Fig. 2(c) shows the final B_z ($z = r$ = 0 mm) value for the ring bulks with *I.D.* = 34 mm for B_{app} = 6.3 and 9.4 T, as a function of *H*. B_z decreases with decreasing *H*. The thinner ring bulks cannot achieve higher trapped fields at the bulk center.

Let us compare the current density distribution for each bulk during FCM. Fig. 3 shows the contour maps of the current distribution, J_θ, along the circumferential (θ) direction in each bulk after the FCM process (*TS* = 10) from B_{app} = 6.3 T. Note that the current flows in the blue region and there is no current in the red region, as defined in Fig. 1. It was found that the current distribution changes depending on the shape of the ring bulks. For the bulks with *H* = 20 mm (bulks (1) – (3)), the supercurrent flows at the periphery and the top and bottom regions of the bulk and the no current region increases with decreasing *I.D.* On the other hand, for the bulks with *I.D.* = 34 mm (bulks (3) – (5)), no current region shrinks with decreasing *H*, and finally the supercurrent flows through the entire bulk cross-section for *H* = 6 mm. The current distribution is closely related to the trapped field profile and determines the final trapped field shown in Fig. 2(a).

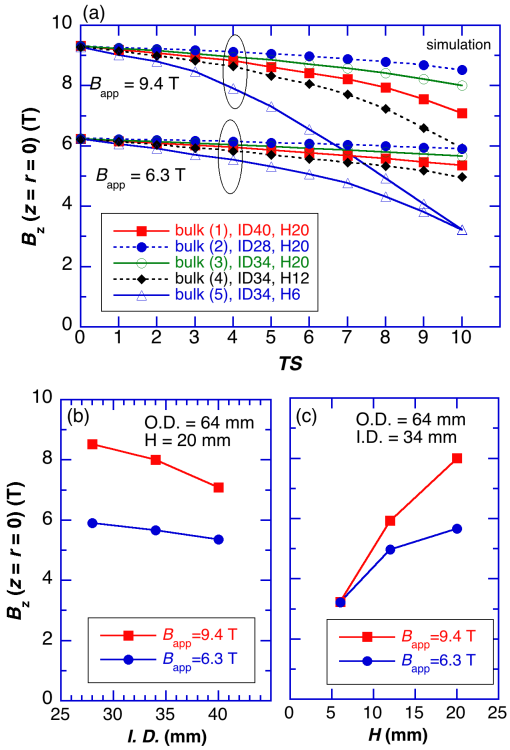

Fig. 2. (a) The *TS* dependence of the trapped field at the center of the five ring bulks, B_z (z = r = 0 mm), during FCM from B_{app} = 6.3 T and 9.4 T. (b) The final B_z (z = r = 0 mm) value for the ring bulks with H = 20 mm for B_{app} = 6.3 and 9.4 T, as a function of *I.D.* and (c) for the ring bulks with *I.D.* = 34 mm, as a function of H.

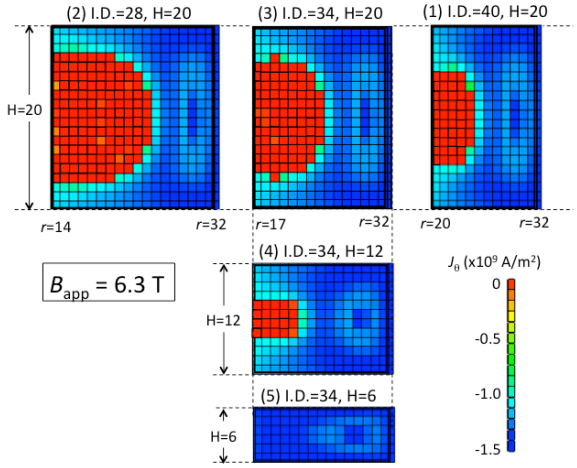

Fig. 3. Contour maps of the current density distribution along the circumferential (θ) direction for each bulk after the FCM process (*TS* = 10) from B_{app} = 6.3 T.

IV. Results of Mechanical Simulation

A. Cooling process

Figs. 4(a) and 4(b), respectively, show the thermal hoop stress profiles, σ_θ^{cool}, at the bulk center (z = 0 mm) and the bulk surface of each bulk after cooling from 300 to 50 K. The shape of the ring bulk influences on σ_θ^{cool} profile. At the bulk center, shown in Fig. 4(a), a large compressive stress is applied to the ring bulk by the Al alloy ring due to the difference in the thermal expansion coefficient [7]. The maximum compressive stress takes place at the bulk periphery (r = 31 mm) for each bulk. On the other hand, on the bulk surface, as shown in Fig. 4(b), the compressive stress at the bulk periphery decreases for all the bulks and changes to a tensile stress for the bulks (1) - (3). The maximum tensile stress was +40 MPa for the smaller *I.D.* bulk (2) (*I.D.* = 28 mm, H = 20 mm) at r = 31 mm.

Fig. 4(c) shows the σ_θ^{cool} value at r = 30 or 31 mm for the ring bulks with H = 20 mm after the cooling to 50 K, as a function of *I.D.*. The σ_θ^{cool} value decreases with increasing *I.D.* Fig. 4(d) shows the σ_θ^{cool} value at r = 30 or 31 mm for the ring bulks with *I.D.* = 34 mm after the cooling to 50 K, as a function of H. The σ_θ^{cool} value on the bulk surface changes from a positive to a negative value with decreasing H and at the bulk center (z = 0 mm), which has a negative (compressive) value, σ_θ^{cool} decreases with decreasing H. In the ring bulk as thin as H = 6 mm, a compressive σ_θ^{cool} is present in all bulk region, although the trapped field is smaller.

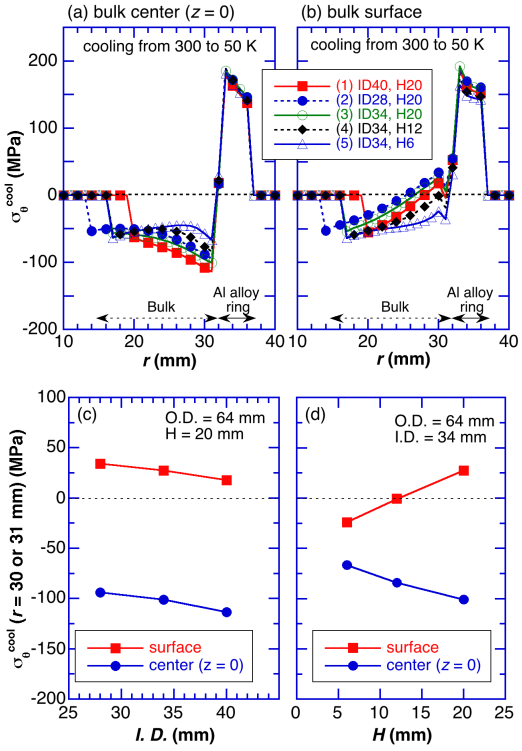

Fig. 4. Thermal hoop stress profiles, σ_θ^{cool}, at (a) the bulk center (z = 0 mm) and (b) the bulk surface, for each bulk during cooling from 300 to 50 K. (c) The σ_θ^{cool} value of the ring bulks at r = 30 or 31 mm with H = 20 mm after cooling to 50 K, as a function of *I.D.* (d) The σ_θ^{cool} value of the ring bulks at r = 30 or 31 mm with *I.D.* = 34 mm after cooling to 50 K, as a function of H.

B. FCM process

Fig. 5(a) shows the time step dependence of electromagnetic hoop stress, σ_θ^{FCM}, during FCM from B_{app} = 9.4 T at the inner edge on the bulk surface for each ring bulk, at which the σ_θ^{FCM} value is the maximum in each bulk [7], [9]. σ_θ^{FCM} increases with increasing *TS*, takes a maximum at an intermediate *TS* and then decreases with the increase in *TS* for each ring bulk, which is a common tendency for σ_θ^{FCM} during FCM. It

should be noted that the σ_θ^{FCM} – *TS* profile for bulk (5) (*I.D.* = 34 mm, *H* = 6 mm) is quite different to that for the other bulks because the supercurrent flows through the entire bulk cross-section.

Fig. 5(b) shows the maximum electromagnetic hoop stress, σ_θ^{FCM}(max), as a function of *I.D.*, for the bulks with *H* = 20 mm, at the bulk center and the bulk surface, during FCM from 6.3 and 9.4 T. σ_θ^{FCM}(max) occurs at the inner edge of each ring bulk and at the bulk surface this is slightly larger than at the bulk center (*z* = 0 mm). Fig. 5(c) shows σ_θ^{FCM}(max) in the bulks of *I.D.* = 34 mm at bulk center and bulk surface during FCM, as a function of *H*. Similar to Fig. 5(b), the difference between the bulk center and bulk surface is very small. σ_θ^{FCM}(max) increases with decreasing *H*, which suggests that the thin ring bulk fractures more easily during FCM.

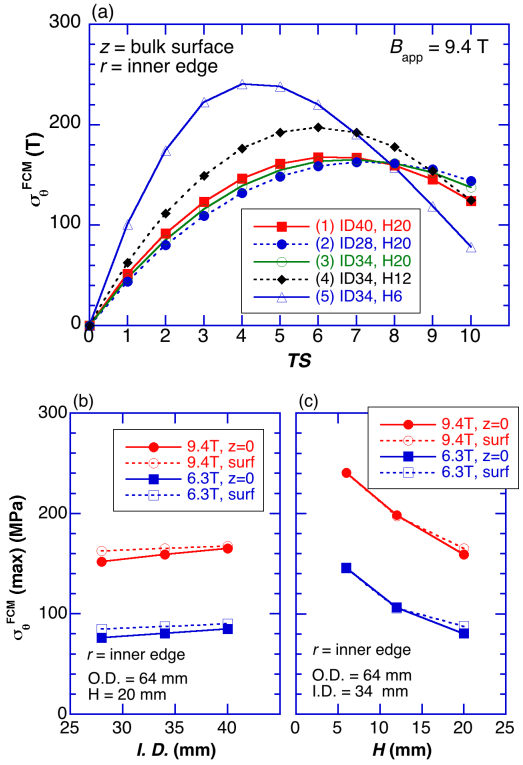

Fig. 5. The *TS* dependence of the electromagnetic hoop stress, σ_θ^{FCM}, during FCM from 9.4 T, at the inner edge on the bulk surface for each ring bulk. (b) Maximum electromagnetic hoop stress, σ_θ^{FCM}(max), in the bulks with *H* = 20 mm, at the bulk center and bulk surface during FCM, as a function of *I.D.* (c) σ_θ^{FCM}(max) in the bulks of *I.D.* = 34 mm at the bulk center and bulk surface during FCM, as a function of *H*.

C. *Cooling + FCM process*

Figs. 6(a) and 6(b), respectively, show the *TS* dependence of the total hoop stress profile, σ_θ^{total} (= σ_θ^{cool} + σ_θ^{FCM}), for bulk (3) (*I.D.* = 34 mm, *H* = 20 mm) at the bulk center (*z* = 0 mm) and at the bulk surface (*z* = 10 mm) during FCM from 9.4 T. The σ_θ^{total} profile at the step 0 shows the σ_θ^{cool} without FCM, as shown in Fig. 4. The maxmum σ_θ^{total} at the bulk center (*z* = 0 mm) occurs at the inner edge (*r* = 17 mm) due to the increase from σ_θ^{FCM}. On the other hand, on the bulk surface (*z* = 10 mm), the maximum σ_θ^{total} takes place at the inner edge (*r* = 17 mm) and also at the bulk edge (*r* = 30 mm). The maximum σ_θ^{total} changes depending on the *TS* dependence of the σ_θ^{cool} and σ_θ^{FCM} values.

Fig. 7(a) shows the *TS* dependence of the total hoop stress, σ_θ^{total}, at the inner edge on the bulk surface for each ring bulk during FCM from B_{app} = 9.4 T, after cooling to 50 K. The σ_θ^{total} values decreased, compared to the σ_θ^{FCM} values, due to the addition of the compressive stress by cooling. However, a tensile stress larger than +100 MPa is present during FCM from 9.4 T, which suggests the possibility of the bulk fracturing, since the fracture strength of typical Ag-doped REBaCuO bulks is considered to be 50 ~ 70 MPa [17], [18].

Fig. 7(b) shows the maximum σ_θ^{total} value for the ring bulks with *H* = 20 mm at the bulk center (*z* = 0 mm) and the bulk surface during FCM from 6.3 and 9.4 T, as a function of *I.D*. The maximum σ_θ^{total} for B_{app} = 9.4 T takes place at the inner edge and the difference is small between the bulk center and surface. However, for B_{app} = 6.3 T, the maximum σ_θ^{total} value at the bulk surface is larger than that at the bulk center, because the σ_θ^{total} value at the periphery of the bulk surface becomes large due to the existence of the tensile stress during the cooling process. Fig. 7(c) shows the maximum σ_θ^{total} value for the ring bulks with *I.D.* = 34 mm at the bulk center (*z* = 0 mm) and the bulk surface during FCM from 6.3 and 9.4 T, as a function of *H*. For a similar reason to that for bulk (3), the maximum σ_θ^{total} value at the bulk surface is larger than that at the bulk center for B_{app} = 6.3 T. However, for smaller *H* values, the maximum σ_θ^{total} value takes place at the inner edge and the difference between the bulk center and the bulk surface is very small.

The results in Figs. 7(b) and 7(c) suggest that the ring bulks reinforced by Al alloy ring, except bulk (5), may avoid mechanical fracture during FCM from 6.3 T, because the maximum σ_θ^{total} value is +62 MPa, which is nearly the same as the fracture strength (50 ~ 70 MPa) of typical REBaCuO bulks [17], [18]. However, bulk (5) (*I.D.* = 34 mm, *H* = 6 mm) during FCM from 6.3 T, and all five bulks during FCM from 9.4 T, must suffer fracture based on the present simulation. To achieve a higher trapped field during FCM from a higher B_{app} without fracture, a new reinforcement method must be applied, which has been proposed elsewhere [10].

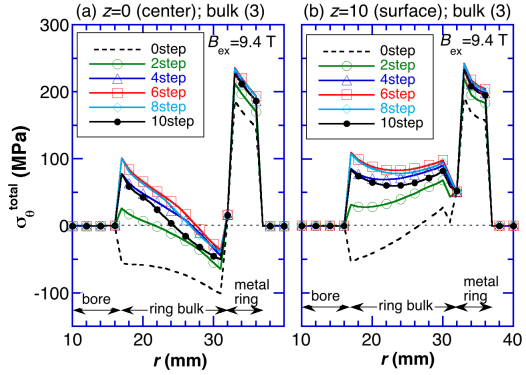

Fig. 6. The *TS* dependence of the total hoop stress profile, σ_θ^{total} (= σ_θ^{cool} + σ_θ^{FCM}), for bulk (3) at (a) the bulk center (*z* = 0 mm) and (b) the bulk surface during FCM from 9.4 T.

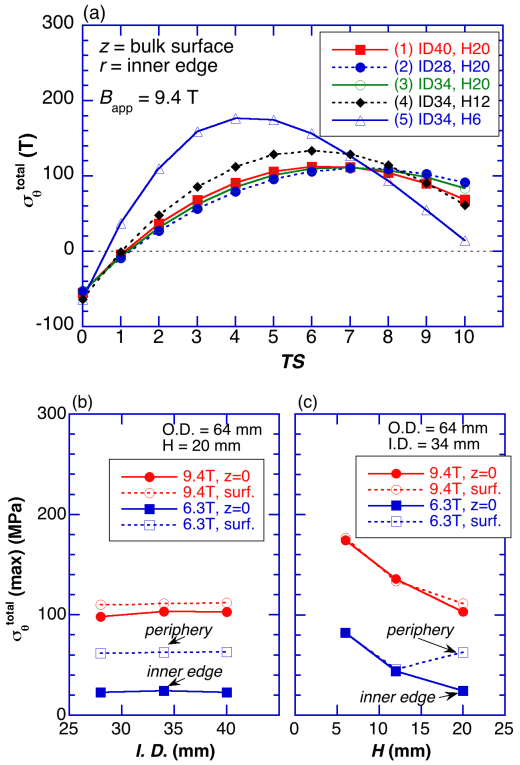

Fig. 7. (a) The *TS* dependence of the total hoop stress, σ_θ^{total}, at the inner edge on the bulk surface for each ring bulk during FCM from B_{app} = 9.4 T after cooling to 50 K. (b) The maximum σ_θ^{total} value for the ring bulks with H = 20 mm at the bulk center (z = 0 mm) and the bulk surface during FCM from 6.3 and 9.4 T, as a function of *I.D.* (c) The maximum σ_θ^{total} value for the ring bulks with *I.D.* = 34 mm at the bulk center and the bulk surface during FCM, as a function of H.

Fig. 8 shows the relationship between the trapped field, B_z, and the maximum total hoop stress, σ_θ^{total}(max), for the five ring bulks for B_{app} = 6.3 and 9.4 T, which was summarized from Figs. 2(a) and 7. It was found that the *I.D.* should be decreased and H should be increased to both enhance the trapped field and reduce the hoop stress simultaneously. This direction means the approach to fabricating a long disk bulk. These results present useful guidelines for designing ring-shaped TFMs to avoid the mechanical fracture. However, to achieve a higher trapped field during FCM from B_{app} = 9.4 T without fracture, a new reinforcement method must be applied [10].

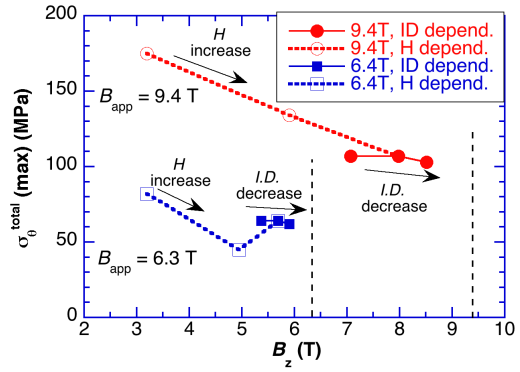

Fig. 8. The relationship between the B_z value and the σ_θ^{total}(max) value for the five cases at B_{app} = 6.3 and 9.4 T.

V. Conclusion

We have investigated numerically the trapped field, B_z, thermal hoop stress, σ_θ^{cool}, by cooling from 300 to 50 K and electromagnetic hoop stress, σ_θ^{FCM}, during FCM from B_{app} = 6.3 and 9.4 T for ring-shaped REBaCuO bulks of various *I.D.* and H, reinforced by an Al alloy ring. The B_z value at the center changes depending on the *I.D.* and H values of the ring bulk, which results from the different superconducting current density distribution. The total hoop stress σ_θ^{total} (= σ_θ^{cool} + σ_θ^{FCM}) also changed at each position and for each B_{app} due to variation of σ_θ^{cool} and σ_θ^{FCM}. The maximum σ_θ^{total} value, which takes place at the innermost edge, decreases with increasing the height of ring bulk. For B_{app} = 6.3 T, the maximum σ_θ^{total} value can be reduced below the fracture strength of 50 ~ 70 MPa of the bulk material. However, for B_{app} = 9.4 T, the ring bulk must break. It is necessary to introduce a new reinforcement structure to avoid the mechanical fracture of the ring bulk to realize the 400 MHz NMR bulk magnet.

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